

Ferromagnetic ordering:

Weiss proposed that in addition to external magnetic field, there is an internal field called the molecular field or Weiss field.

For paramagnet, $y = g_J \mu_B \frac{B J}{k_B T}$ $B = \text{ext. field,}$

In the presence of molecular field,

~~$B \approx \text{ext. field} + \text{molecular field}$~~

$$y = g_J \mu_B \frac{(B + \lambda M) J}{k_B T}$$

Even for external field $B=0$, there is spontaneous magnetization due to AM.

$$y = g_J \mu_B \frac{\lambda M J}{k_B T}$$

So, the

$$\frac{M}{M_s} = B_J(y) = B_J\left(\frac{g_J \mu_B \lambda M J}{k_B T}\right) \quad \text{--- (1)}$$

$$y = \frac{g_J \mu_B \lambda M J}{k_B T}$$

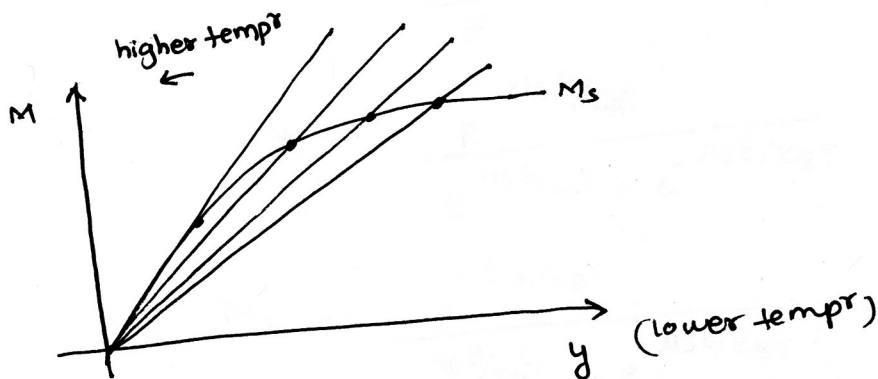
$$\text{or } M = \frac{y k_B T}{g_J \mu_B \lambda J} \quad \text{--- (2)}$$

linear dependence with y ,

$$\text{with slope} = \frac{k_B}{g_J \mu_B \lambda J} T \quad \text{--- (3)}$$

$\propto T$

higher the temp, higher or steeper will be the slope



From graph we see that point of intersection is the solution to both eqn (1) & (2), i.e. it gives the Magnetization for certain value of y .

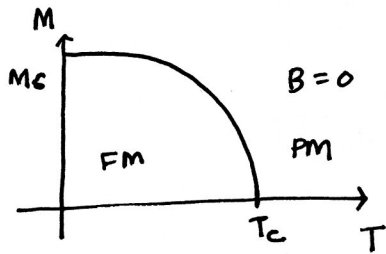
We also see that higher the temperature larger will be the slope.

And for certain critical temperature, slope of the line is equal to the slope of the Brillouin function ~~at $y=0$~~ , and $y=0$ is the only solⁿ.

This critical temperature at which the magnetization ~~is zero~~ is called the Curie Temperature T_c .

For Temperature $T > T_c$ ~~constant~~, only solⁿ is $M=0$ at $y=0$

For temperature $T < T_c$ (spontaneous magnetization is found).



To find T_c , we find slope of Brillouin function at $y \rightarrow 0$

We know, At $y \rightarrow 0$ (smallly) $B_J(y) \approx y \left(\frac{J+1}{3J} \right)$

So slope of $B_J(y)$ $\frac{dM}{dy} = M_s \left(\frac{J+1}{3J} \right)$

At critical temperature, slope of Brillouin fn = slope of line from (3)

$$\frac{k_B T_c}{g_J \mu_B \lambda J} = M_s \left(\frac{J+1}{3J} \right)$$

$$\Rightarrow T_c = \frac{(g_J \mu_B J)}{k_B} \lambda M_s \left(\frac{J+1}{3J} \right)$$