

Solutions

PHYS-203A-002

(Final Exam)

Fall 2021

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Problem 1

$$\begin{aligned} 9.8 \frac{\text{m}}{\text{s}^2} &= 9.8 \frac{\text{m}}{\text{s}^2} \left(\frac{3600 \text{ s}}{1 \text{ hour}} \right)^2 \\ &= 9.8 (3600)^2 \frac{\text{meter}}{\text{hour}^2} = 1.3 \times 10^8 \frac{\text{meter}}{\text{hour}^2} \end{aligned}$$

Problem 2

50.0 $\frac{\text{m}}{\text{s}}$. There is no acceleration in horizontal direction.

Problem 3

No, circular motion requires acceleration.

Problem 4

Solid cylinder, because it has a smaller moment of inertia I .

Problem 5

$$\Delta y = 15 \text{ m}$$

$$\Delta t = ?$$

$$v_i = \text{missing}$$

$$v_f = 0$$

$$a = -9.8 \frac{\text{m}}{\text{s}^2}$$

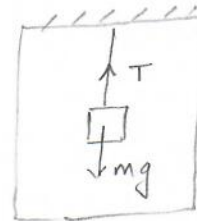
$$\begin{aligned} \Delta y &= v_f \Delta t - \frac{1}{2} a \Delta t^2 \\ 15 &= 0 - \frac{1}{2} (-9.8) \Delta t^2 \end{aligned}$$

$$\Delta t = 1.8 \text{ seconds.}$$

Problem 6

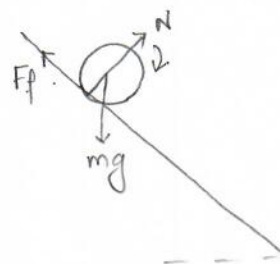
$$ma = T - mg$$

$$\begin{aligned} T &= ma + mg \\ &= (5.0)(2.0) + (5.0)(9.8) \\ &= 59 \text{ Newton} \end{aligned}$$



Problem 7

Linear work and rotational work
done by force of friction cancel.



$$\underbrace{\frac{1}{2} M v_i^2}_{=0} + \underbrace{\frac{1}{2} I \omega_i^2}_{=0} + Mg h_i = \frac{1}{2} M v_f^2 + \frac{1}{2} I \omega_f^2 + \underbrace{Mg h_f}_{=0}$$

$$\begin{aligned} Mg h_i &= \frac{1}{2} M v_f^2 + \frac{1}{2} I \omega_f^2 \\ &= \frac{1}{2} M v_f^2 + \frac{1}{5} M v_f^2 \end{aligned}$$

$$\begin{aligned} \frac{1}{2} I \omega_f^2 &= \frac{1}{2} \left(\frac{2}{5} M R^2 \right) \omega_f^2 \\ &= \frac{1}{5} M v_f^2 \end{aligned}$$

$$Mg h_i = \frac{7}{10} M v_f^2$$

$$v_f = \sqrt{\frac{10}{7} g h_i}$$

$$= \sqrt{\frac{10}{7} (9.8)(1.20)}$$

$$= 4.1 \frac{\text{m}}{\text{s}}$$

Problem 8

$$\begin{aligned}
 U &= - \frac{G M_1 M_2}{r} \\
 &= - \frac{(6.7 \times 10^{-11}) (6 \times 10^{24}) (8 \times 10^{27})}{(6 \times 10^9)} \\
 &= - 6 \times 10^{30} \text{ J}
 \end{aligned}$$

You will need $6 \times 10^{30} \text{ J}$ of energy.

$$56 \times 10^{-11-11+24+27}$$

$$56 \times 10^{29}$$

Problem 9

$$\begin{aligned}
 U &= U_{12} + U_{13} + U_{23} \\
 &= - \frac{GM^2}{L} - \frac{GM^2}{L} - \frac{GM^2}{L} \\
 &= - 3 \frac{GM^2}{L}
 \end{aligned}$$

