

Solutions

PHYS-203A

(Midterm Exam 03) Fall 2021

①

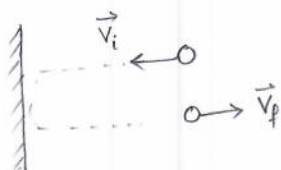
Problem 1

No, $W_N \neq 0$ because the displacement of the object is in the direction of the normal force.

Problem 2

$W_g = 0$, because it is a round trip.

Problem 3



$$\vec{v}_f = +\hat{i} 5.0 \frac{\text{m}}{\text{s}}$$

$$\vec{v}_i = -\hat{i} 5.0 \frac{\text{m}}{\text{s}}$$

$$\vec{J} = m \vec{v}_f - m \vec{v}_i$$

$$= (0.050) \hat{i} 5.0 - (-\hat{i}) (0.050) 5.0$$

$$= \hat{i} 0.50 \text{ kg } \frac{\text{m}}{\text{s}}$$

Problem 4

$$v = \omega R$$

(perfect rolling)

$$v > \omega R$$

(sliding)

$$v < \omega R$$

(slipping)

Problem 5

$$\Delta K = W_g + W_N \quad W_N = 0$$

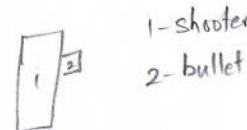
$$\begin{aligned} W_g = \Delta K &= \frac{1}{2} m v_E^2 - \frac{1}{2} m v_c^2 \\ &= \frac{1}{2} (500.0) (12)^2 - \frac{1}{2} (500.0) (8.0)^2 \\ &= 2.0 \times 10^4 \text{ J} \end{aligned}$$

Problem 6

$$m_1 v_{1i} + m_2 v_{2i} = m_1 v_{1f} + m_2 v_{2f}$$

$$0 + 0 = m_1 v_{1f} + m_2 v_{2f}$$

$$\begin{aligned} v_{1f} &= -\frac{m_2}{m_1} v_{2f} \\ &= -\frac{(0.0050)}{75} (600.0) = -0.040 \frac{\text{m}}{\text{s}} = -4.0 \frac{\text{cm}}{\text{s}} \end{aligned}$$



Problem 7

$$\begin{aligned} v_{1f} &= \left(\frac{m_1 - m_2}{m_1 + m_2} \right) v_{1i} + \left(\frac{2 m_2}{m_1 + m_2} \right) v_{2i} \\ &= \left(\frac{25 - 75}{25 + 75} \right) (+4.0) + \frac{2(75)}{(25 + 75)} (0) \\ &= -2.0 \frac{\text{m}}{\text{s}} \end{aligned}$$

$$\begin{aligned} v_{2f} &= \left(\frac{2 m_1}{m_1 + m_2} \right) v_{1i} + \left(\frac{m_2 - m_1}{m_1 + m_2} \right) v_{2i} \\ &= \frac{2(25)}{(25 + 75)} (+4.0) + \left(\frac{75 - 25}{25 + 75} \right) (0) \\ &= +2.0 \frac{\text{m}}{\text{s}} \end{aligned}$$

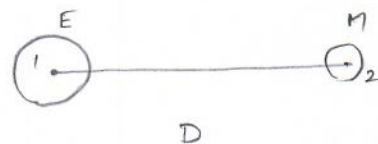


Problem 8

$$x_{cm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2}$$

$$= \frac{0 + (7.4 \times 10^{22}) 60. R_E}{(600 \times 10^{22} + 7.4 \times 10^{22})}$$

$$= 0.73 R_E = 4.7 \times 10^6 \text{ m} \rightarrow \text{from center of Earth.}$$



$$D = 3.84 \times 10^8 \text{ m}$$

$$= \frac{3.84 \times 10^8}{6.4 \times 10^6} R_E = 60. R_E$$

Problem 9

$$\Delta \theta =$$

$$\Delta t = 8.00 \text{ s}$$

$$\omega_i = 0$$

$$\omega_f = 75.0 \frac{\text{rad}}{\text{s}}$$

$$\alpha = ?$$

$$\alpha = \frac{\omega_f - \omega_i}{\Delta t} = \frac{75.0 - 0}{8.00} = 9.4 \frac{\text{rad}}{\text{s}^2}$$